



If  $y = -3x^2 - 2x + 1$ , use the definition of a derivative to determine  $y'$ .

$$\lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} \quad \begin{array}{l} f(4) \\ -3(4)^2 - 2(4) + 1 \end{array}$$

$$\lim_{h \rightarrow 0} \frac{-3(x+h)^2 - 2(x+h) + 1 - (-3x^2 - 2x + 1)}{h}$$

$$\lim_{h \rightarrow 0} \frac{-3(x^2 + 2xh + h^2) - 2x - 2h + 1 + 3x^2 + 2x - 1}{h}$$

$$\lim_{h \rightarrow 0} \frac{-3x^2 - 6xh - 3h^2 - 2h + 3x^2}{h}$$

$$\lim_{h \rightarrow 0} \frac{-6xh - 3h^2 - 2h}{h}$$

$$\lim_{h \rightarrow 0} \frac{h(-6x - 3h - 2)}{h}$$

$$f'(x) = -6x - 2$$



$$y = x^2$$
$$y' = 2x$$

$$y = 2x^2 - 5x + 6$$
$$y' = 4x - 5$$

$$y = -3x^2 - 2x + 1$$
$$y' = -6x - 2$$

$$y = 8x^2 + 10x - 8$$
$$y' = 16x + 10$$

Calculus 120

Unit 1: Rate of Change and Derivatives

February 8, 2019: Day #7

1. Assignment Due on Wednesday

2. Quick Quiz <sup>wednesday</sup> ~~Tuesday~~ on Derivatives

## **Curriculum Outcomes**

**C1.** Explore the concepts of average and instantaneous rate of change.

Ex:

Find  $y'$  and the slope of the tangent line at  $x = -5$  for  $f(x) = x^3 + x + 2$ 

$$\lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$\lim_{h \rightarrow 0} \frac{(x+h)^3 + x+h + 2 - (x^3 + x + 2)}{h}$$

$$\lim_{h \rightarrow 0} \frac{\cancel{x^3} + 3x^2h + 3xh^2 + \cancel{h^3} + \cancel{x+h+2} - \cancel{x^3} - \cancel{x} - \cancel{2}}{h}$$

$$\lim_{h \rightarrow 0} \frac{3x^2h + 3xh^2 + h^3 + h}{h}$$

$$\lim_{h \rightarrow 0} \cancel{h} (3x^2 + 3xh + h^2 + 1)$$

$$f'(x) = 3x^2 + 1$$

$$f'(-5) = 3(-5)^2 + 1$$

$$m = 76$$

$$\begin{aligned} & (x+h)^3 \\ & (x+h)(x+h)(x+h) \\ & (\cancel{x+2xh+h^2})(x+h) \\ & \underbrace{x^3 + x^2h + 2x^2h}_{\sim} + 2xh^2 + xh^2 + h^3 \end{aligned}$$

If  $f(x) = \sqrt{x+2}$ , find  $f'(x)$ . State the domains of  $f$  and  $f'$ .

Domain:  $[-2, \infty)$

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$\frac{(x-3)(x+5)}{x^2 - 25}$$

$$= \lim_{h \rightarrow 0} \left( \frac{\sqrt{x+h+2} - \sqrt{x+2}}{h} \right) \left( \frac{\sqrt{x+h+2} + \sqrt{x+2}}{\sqrt{x+h+2} + \sqrt{x+2}} \right)$$

$$= \lim_{h \rightarrow 0} \frac{\cancel{x+h+2} - (\cancel{x+2})}{h(\sqrt{x+h+2} + \sqrt{x+2})}$$

$$= \lim_{h \rightarrow 0} \frac{h}{h(\sqrt{x+h+2} + \sqrt{x+2})}$$

$$= \lim_{h \rightarrow 0} \frac{1}{\sqrt{x+h+2} + \sqrt{x+2}}$$

$$= \frac{1}{\sqrt{x+2} + \sqrt{x+2}}$$

$$f'(x) = \frac{1}{2\sqrt{x+2}} \rightarrow \text{Domain: } (-2, \infty)$$

Find  $f'$  if  $f(x) = \frac{x+1}{3x-2}$ . Determine the equation the tangent line to  $f(x)$  at  $x = 1$  and the equation of the normal line to  $f(x)$  at  $x = 1$ .

$$\lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$\lim_{h \rightarrow 0} \frac{\frac{x+h+1}{3(x+h)-2} - \frac{x+1}{3x-2}}{h}$$

$$\lim_{h \rightarrow 0} \left( \frac{\frac{x+h+1}{3x+3h-2} \cdot \frac{3x-2}{3x-2} - \frac{x+1}{3x-2} \cdot \frac{3x+3h-2}{3x+3h-2}}{h} \right)$$

$$\lim_{h \rightarrow 0} \frac{\cancel{3x^2} - \cancel{2x} + \cancel{3xh} - \cancel{2h} + \cancel{3x-2} - (\cancel{3x^2} + \cancel{3xh} - \cancel{2x} + \cancel{3x+3h-2})}{h(3x+3h-2)(3x-2)}$$

$$\lim_{h \rightarrow 0} \left( \frac{-5h}{(3x+3h-2)(3x-2)} \right) \left( \frac{1}{h} \right)$$

$$\lim_{h \rightarrow 0} \frac{-5}{(3x+3h-2)(3x-2)}$$

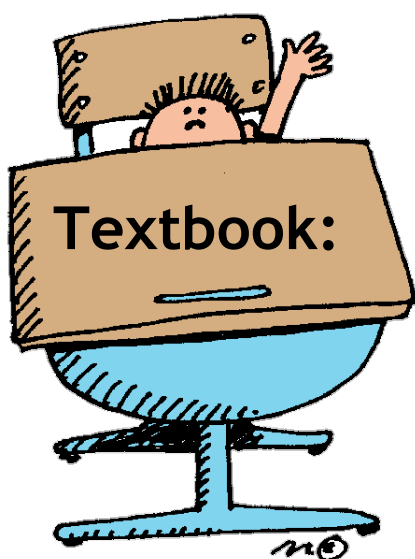
$$f'(x) = \frac{-5}{(3x-2)^2}$$

$$f'(x) = \frac{(3x-2)(1) - (x+1)(3)}{(3x-2)^2}$$

$$= \frac{\cancel{3x-2} - \cancel{3x-3}}{(3x-2)^2}$$

$$= \frac{-5}{(3x-2)^2}$$

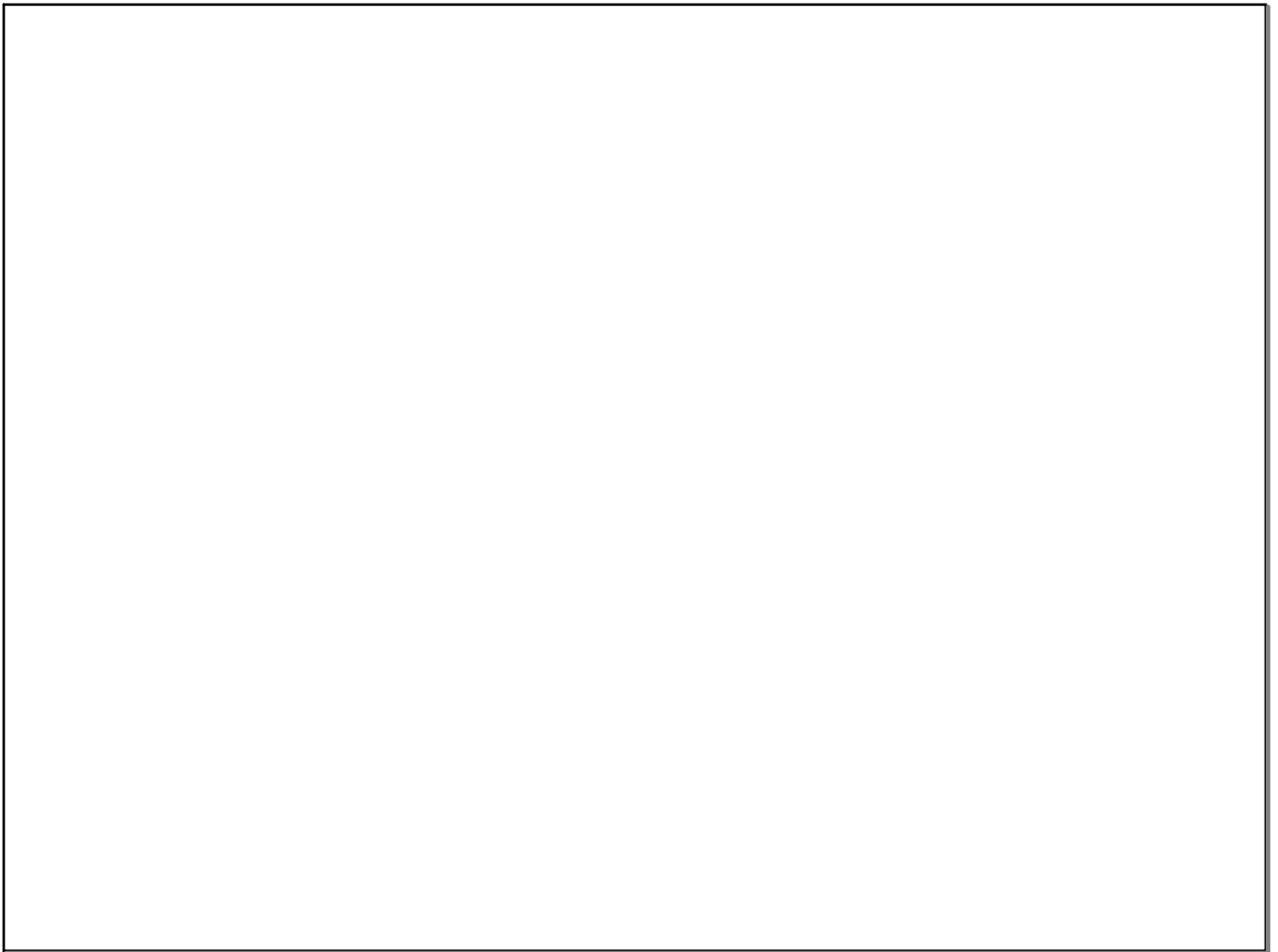




## Practice

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#1, 3, 7, 9, 10, 11, 12, 17,  
18, 19



## Attachments

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2.1\_74\_AP.html



2.1\_74\_AP.swf



2.1\_74\_AP.html